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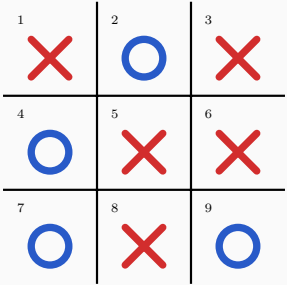
Construction for draw:



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Statistics: 99 submissions, 68 accepted