

# Freshmen Programming Contests 2025

Solutions presentation

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By the Freshmen Programming Contests 2025 jury for:

- AAPJE in Amsterdam
- FPC in Delft
- FYPC in Eindhoven
- GAPC in Groningen
- Contest in Mons

May 3, 2025



Please do not post the problems online

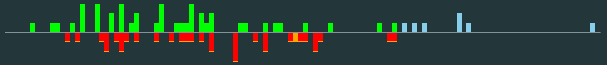
Other universities will have their contests in the coming weeks.

Please, do not post/discuss the problems online before

Saturday 17 May 2025 at 17:00

# G: Gambler's Dilemma

Problem author: Wietze Koops



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**Running time:**  $\mathcal{O}(1)$ .

Statistics: 82 submissions, 42 accepted, 7 unknown

# B: Bakfiets

Problem author: Jeroen Op de Beek

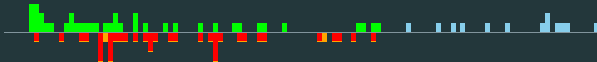


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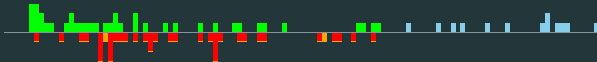


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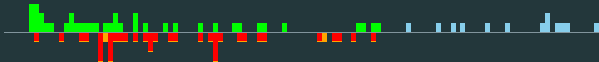
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**Problem:** Minimize the area of one rectangle that cannot overlap with another.

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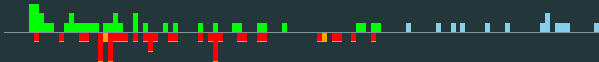


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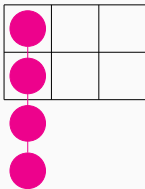


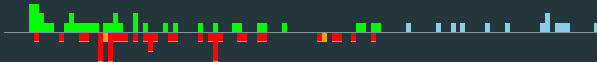
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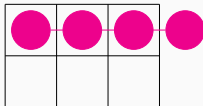


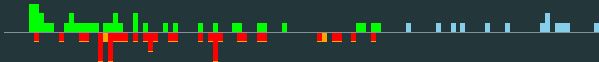
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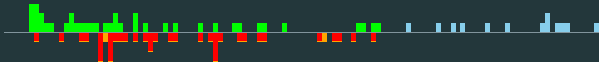


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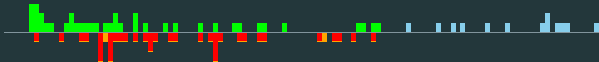
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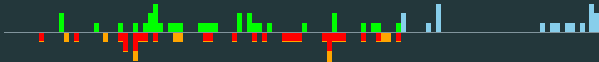
**Running time:**  $\mathcal{O}(1)$ .

Statistics: 90 submissions, 39 accepted, 13 unknown



# J: Jumbled Keys

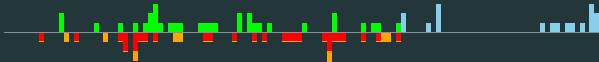
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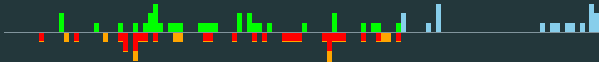
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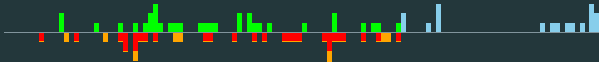
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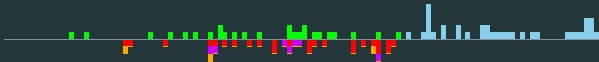
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Statistics: 86 submissions, 33 accepted, 17 unknown

# H: Hopelessly Hungover

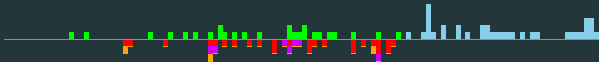
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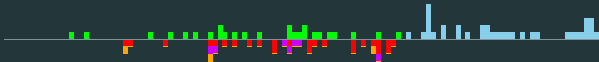


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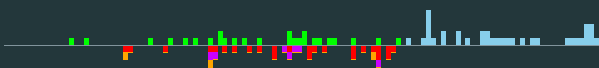
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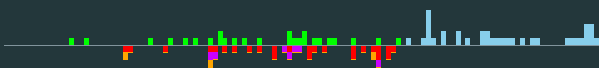
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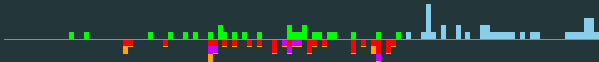
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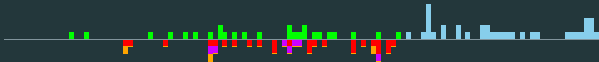
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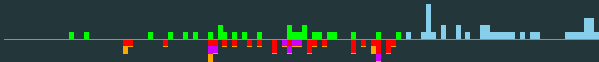
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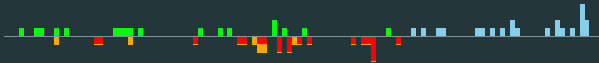
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Statistics: 97 submissions, 26 accepted, 36 unknown

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Statistics: 66 submissions, 18 accepted, 22 unknown

# D: Delicious Trees

Problem author: Jeroen Op de Beek



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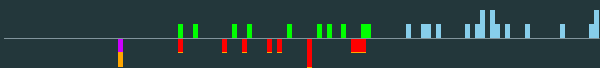


**Problem:** Find any way to cut the AVL tree into some predetermined number of smaller AVL trees, or say this is impossible.

**Observation 1:** An AVL tree with only one vertex, is also an AVL tree.

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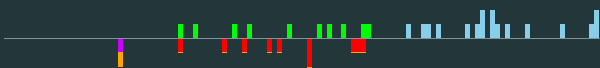
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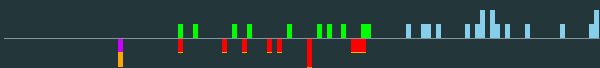
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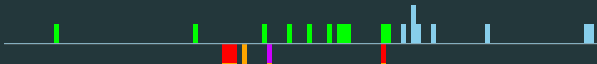
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Statistics: 39 submissions, 10 accepted, 17 unknown

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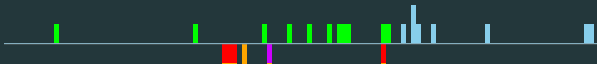
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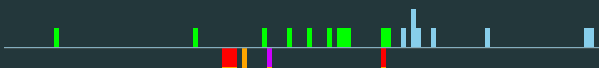


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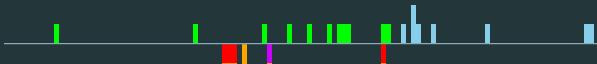
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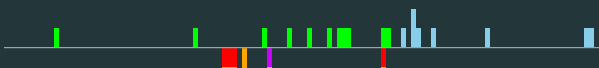
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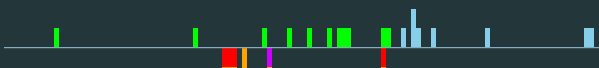
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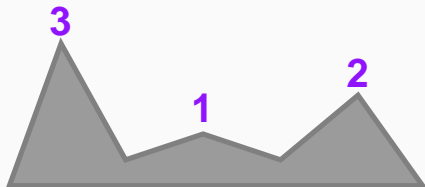
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Statistics: 86 submissions, 5 accepted, 66 unknown

# I: Interesting Mountains

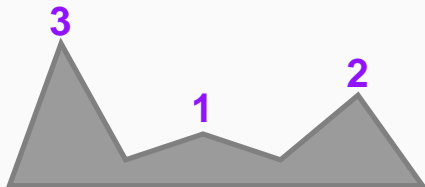
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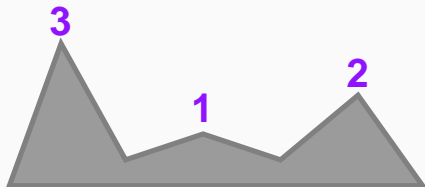


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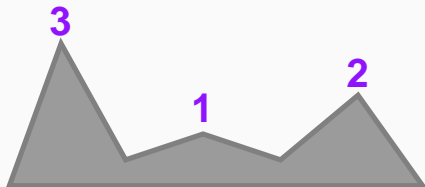
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Let's first learn how to count **inversions**.

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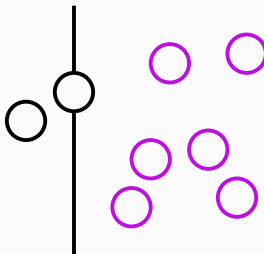
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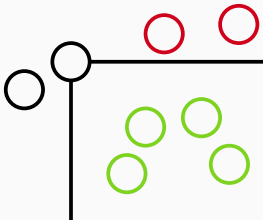
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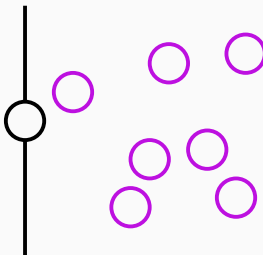
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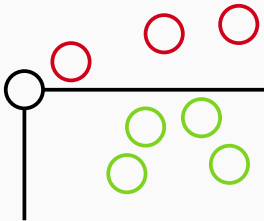
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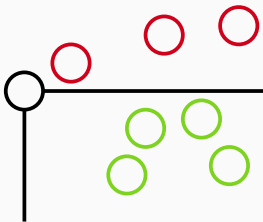
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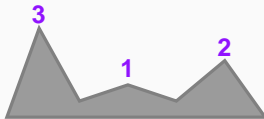
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Using Fenwick tree or segment tree,  $\mathcal{O}(\log(n))$  per query / update.

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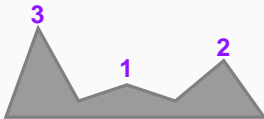
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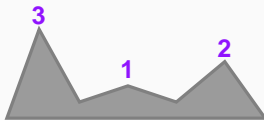
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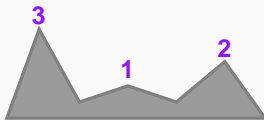
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**However:** This way, we don't distinguish between  $h_i > h_k > h_j$  and  $h_i > h_j > h_k$ :



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**Running time:** We have  $\mathcal{O}(n)$  calls to a Fenwick tree / segment tree, so  $\mathcal{O}(n \log(n))$  total.

Statistics: 22 submissions, 1 accepted, 14 unknown

# K: Kite Construction

Problem author: Jeroen Op de Beek

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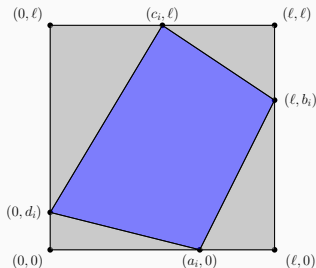
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**Solution:** Let  $(a_i, 0)$ ,  $(\ell, b_i)$ ,  $(c_i, \ell)$  and  $(0, d_i)$  be the coordinates of the corners of the  $i$ th quadrilateral. Then we can compute the sum of the areas by considering how much is cut off from the full  $\ell \times \ell$  square:

$$\sum_{i=1}^n \left( \ell^2 - \frac{1}{2}a_id_i - \frac{1}{2}(\ell - a_i)b_i - \frac{1}{2}(\ell - b_i)(\ell - c_i) - \frac{1}{2}c_i(\ell - d_i) \right).$$



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**Insight:** First consider minimizing  $\sum_{i=1}^n \frac{1}{2}a_i d_i$  only. To do this, we should sort the  $d_i$  in the other order, i.e. such that  $d_1 > d_2 > \dots > d_n$ .

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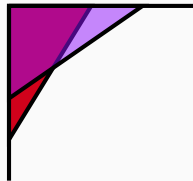
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**Proof:** Suppose that  $i < j$  (and hence  $a_i < a_j$ ), but  $d_i < d_j$ . Then

$$a_i d_j + a_j d_i = a_i d_i + a_j d_j + \underbrace{(a_i - a_j)}_{>0} \underbrace{(d_j - d_i)}_{<0},$$

so swapping  $d_i$  and  $d_j$  would lead to a smaller area cut off.

Hence, whenever  $i < j$  we have  $d_i > d_j$ .



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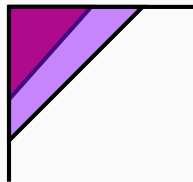
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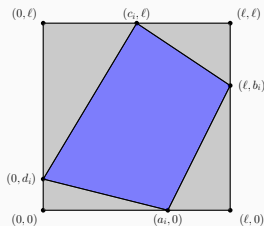
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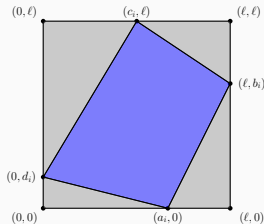
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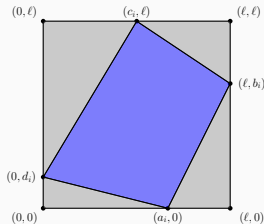
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**Running time:**  $\mathcal{O}(n \log n)$ .

Statistics: 7 submissions, 0 accepted, 7 unknown

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**Problem:** For every divisor  $d$  of  $n$ , find the minimum number of changes to make  $t = t' \odot d$  for some string  $t'$ .



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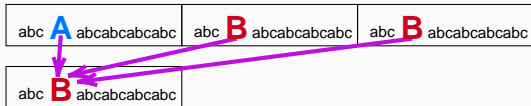
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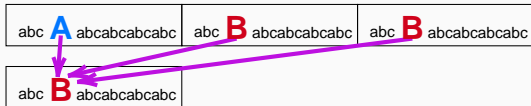


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- Then count how many letters we must have changed.

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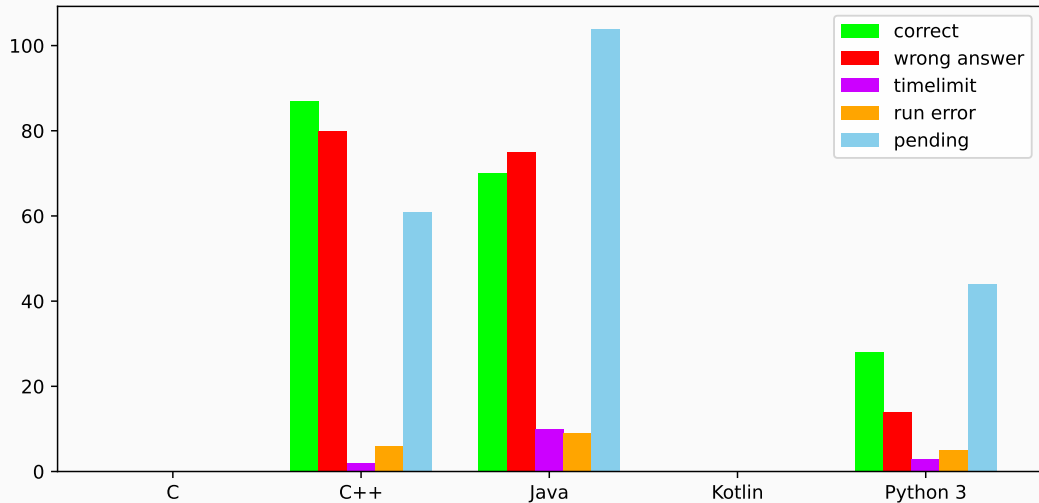
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Statistics: 2 submissions, 0 accepted, 2 unknown

## Language stats



### Jury work

- 423 commits (last year: 447)

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## Random facts

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-

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- The minimum<sup>1</sup> number of lines the jury needed to solve all problems is

$$2 + 1 + 6 + 5 + 1 + 5 + 2 + 2 + 6 + 3 + 6 = 39$$

On average 3.5 lines per problem, down from 6.0 last year

---

<sup>1</sup>After codegolfing

## Thanks to the proofreaders:

- Arnoud van der Leer (TU Delft)
- Dany Sluijk (TU Delft)
- Davina van Meer (Delft)
- Mattia Marziali (RU Groningen)
- Michael Zündorf   
(KIT Karlsruhe / NWERC jury)
- Pavel Kunyavskiy (JetBrains Amsterdam)
- Pierre Vandenhove (UMons)
- Thomas Verwoerd  
(TU Delft,  Kotlin Hero )
- Thore Husfeldt (ITU Copenhagen / BAPC Jury)
- Wendy Yi (KIT Karlsruhe / NWERC jury)

## Thanks to the Jury for the Freshmen Programming Contests:

- Alice Sayutina (VU Amsterdam)
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- Jeroen Op de Beek (TU Delft)
- Leon van der Waal (TU Delft)
- Liudas Staniulis (VU Amsterdam)
- Maarten Sijm (TU Delft)
- Mihail Bankov (TU Delft)
- Moham Balfakeih (TU Delft)
- Wietze Koops (Radboud Nijmegen / RU Groningen)





Want to solve the problems you could not finish?  
Or have friends that like to solve algorithmic problems?

<https://fpcs2025.bapc.eu/>

Saturday 17 May 2025 13:00–17:00

Please, do not post/discuss the problems online before this time!

Excited to participate in the next contest?

Register for DAPC (20 September) at [wisv.ch/dapc](https://wisv.ch/dapc)

Want to organize these contests?

Join the CHipCie: [wisv.ch/chipcieinterest](https://wisv.ch/chipcieinterest)

Want to create programming problems for FPC next year?

Either join the CHipCie, or contact Maarten Sijm