

# Freshmen Programming Contest 2023

Solutions presentation

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May 27, 2023



# A: Admiring Droplets

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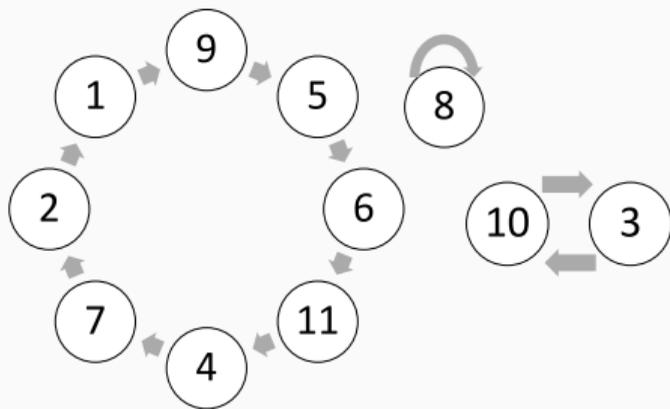
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# F: Feline Friendship

Problem Author: Jeroen Op de Beek

- **Problem:** Given a special functional graph, change the least number of edges such that there is a maximal path of length  $k$ .
- **Observation 1:** The array in the input is a permutation  $\rightarrow$  the favourite cat relations form disjoint cycles.

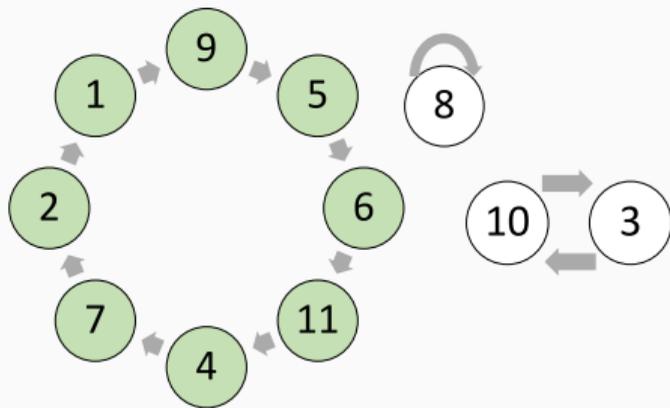


Cats are visualised as circles, with arrows being the favourite playing cat relations

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- **Observation 2:** If there is a cycle of length  $k$ , 0 operations suffice.

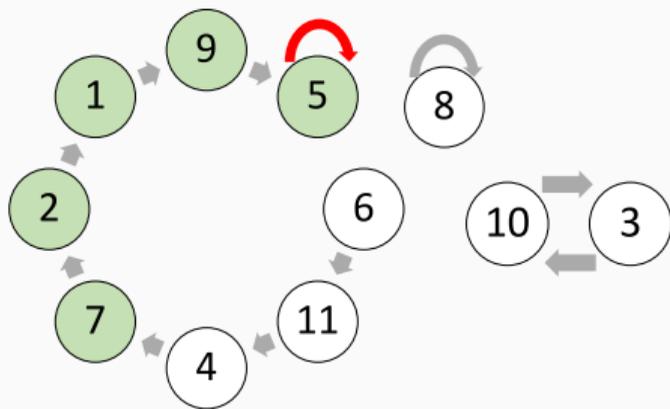


Take whole cycle as team.

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- **Observation 3:** Else if there is a cycle of length  $> k$ , 1 operation is enough.

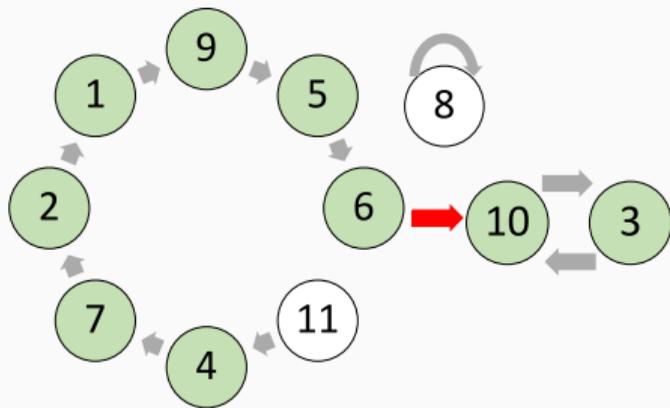


Make cycle into a path, and then choose where to start.

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- **Observation 4:** If you can make teams of length  $a$  and  $b$ , can make team of length  $a + 1, a + 2, \dots, a + b$  in 1 operation.



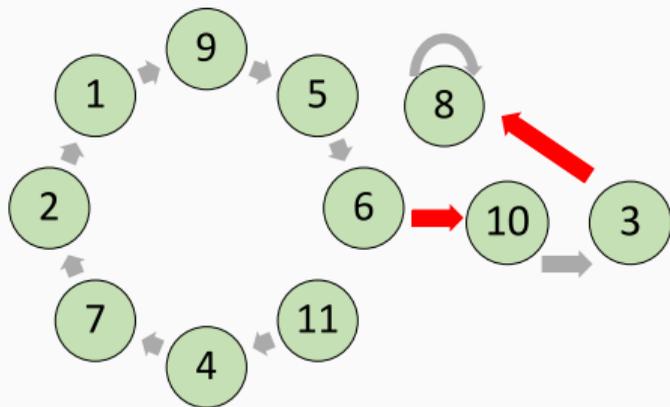
Merge two cycles.



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- **Solution:** Greedily merge largest cycles in this way, until sum becomes  $\geq k$ .
- **Complexity:**  $\mathcal{O}(n)$  for finding the disjoint cycles and  $\mathcal{O}(n \log n)$  or  $\mathcal{O}(n)$  for sorting the cycle sizes.



Repeatedly connect cycles together.

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# G: Gridlock

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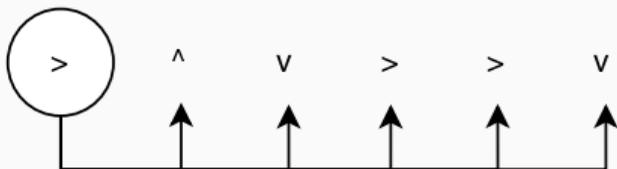
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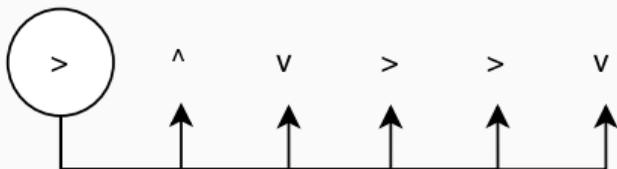
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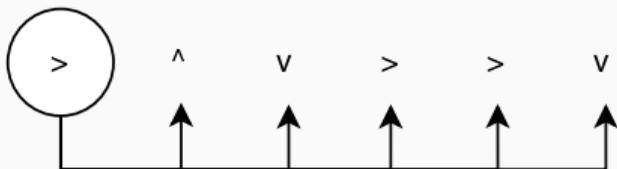


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- **Naive Solution:** We can build a graph with all the dependencies, then compute the topological sorting.
  - If one such sorting exists, we have a solution.
  - If one does not exist, then it is impossible to solve the puzzle.

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- **Naive Solution:** We can build a graph with all the dependencies, then compute the topological sorting.
- **Complexity:**
  - Since an arrow points to an entire row or column of arrows, a cell has  $\mathcal{O}(h)$  or  $\mathcal{O}(w)$  dependencies, therefore, we have  $\mathcal{O}(hw)$  nodes and  $\mathcal{O}(hw(h+w))$  edges.

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  - Since the topological sorting has  $\mathcal{O}(V + E)$  complexity, then this solution yields  $\mathcal{O}(hw(h+w))$  complexity, which is not enough to pass the time limit.

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- **Observation:** Maybe we can try to solve this in the opposite way.
- Instead of starting from a cell and recursively solving all of its dependencies, we can instead start from the trivial nodes, with no dependencies and then solve the nodes with more dependencies.

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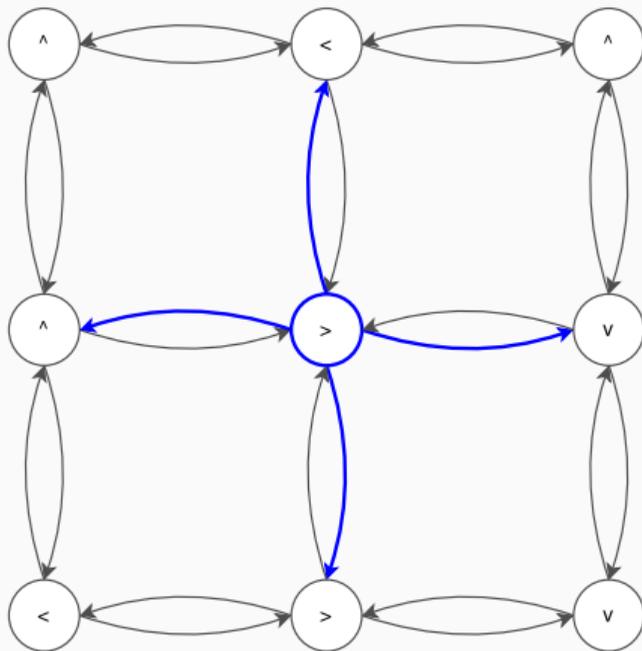
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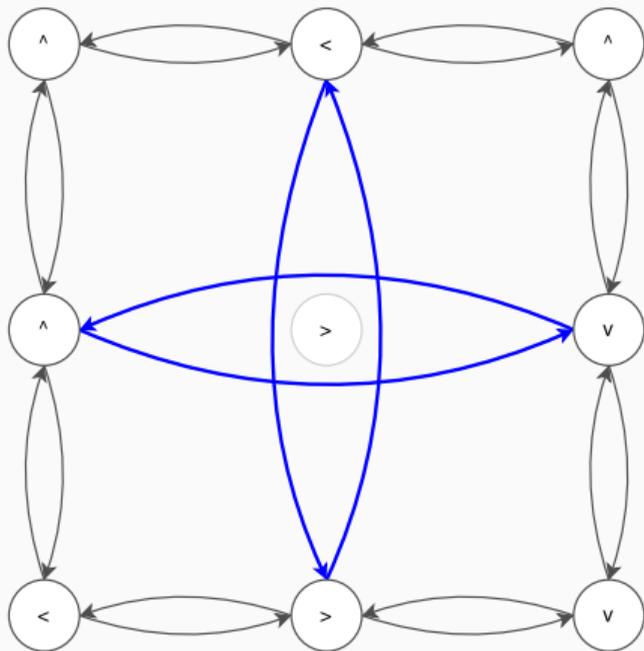
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- When removing a cell, we must link its left and right neighbours between each other. The same goes for the neighbours from above and below.



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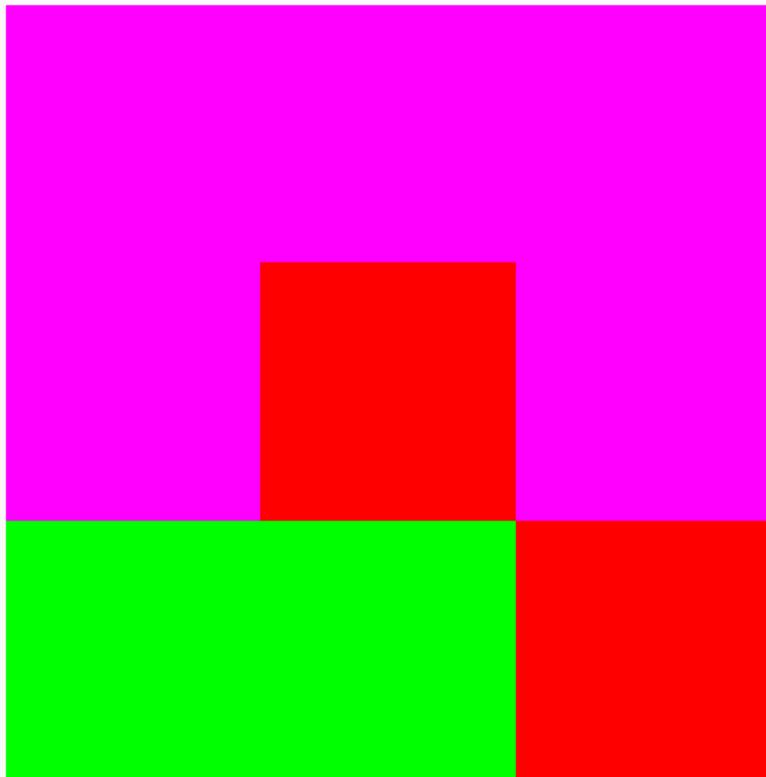
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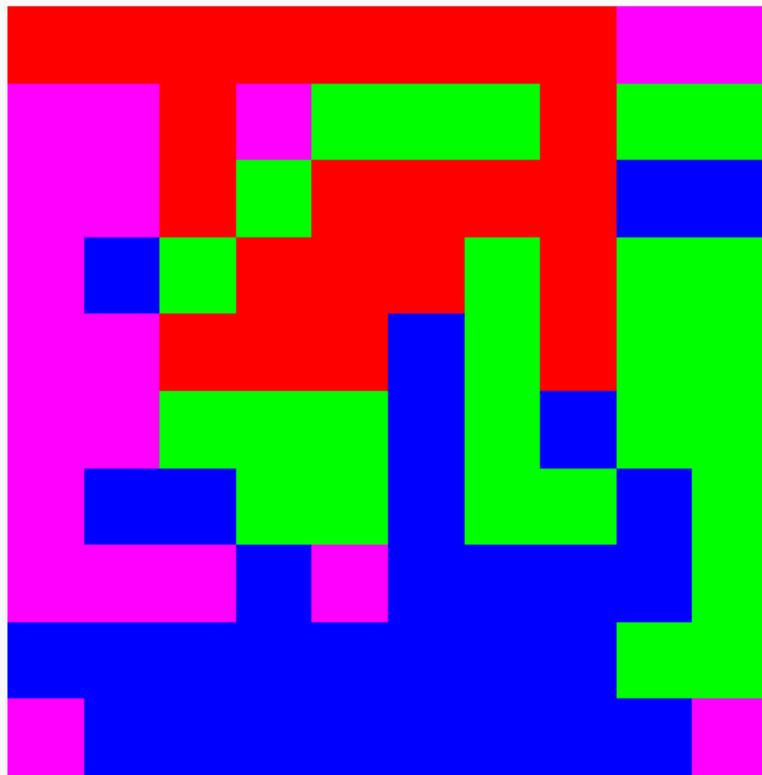
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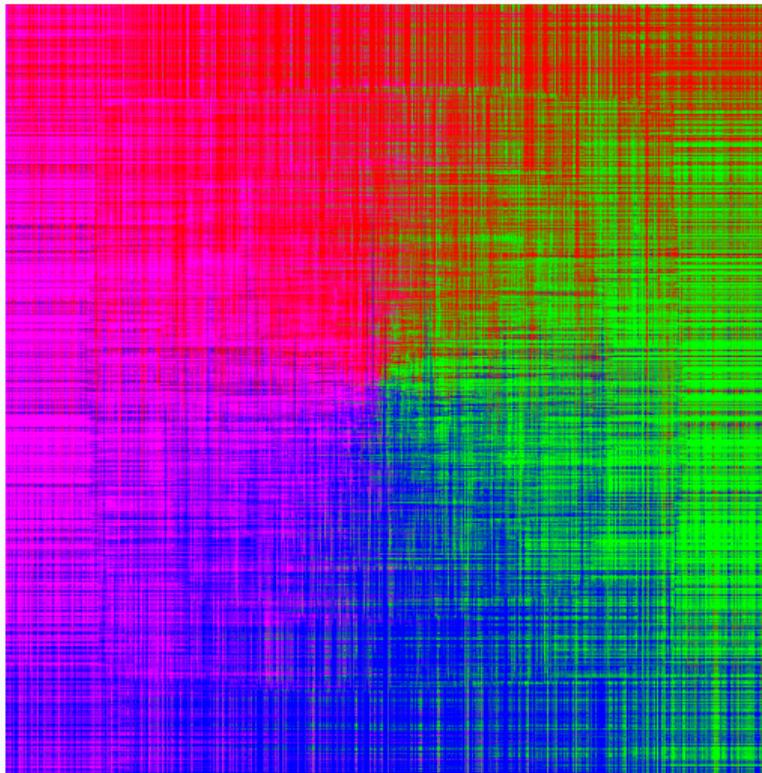
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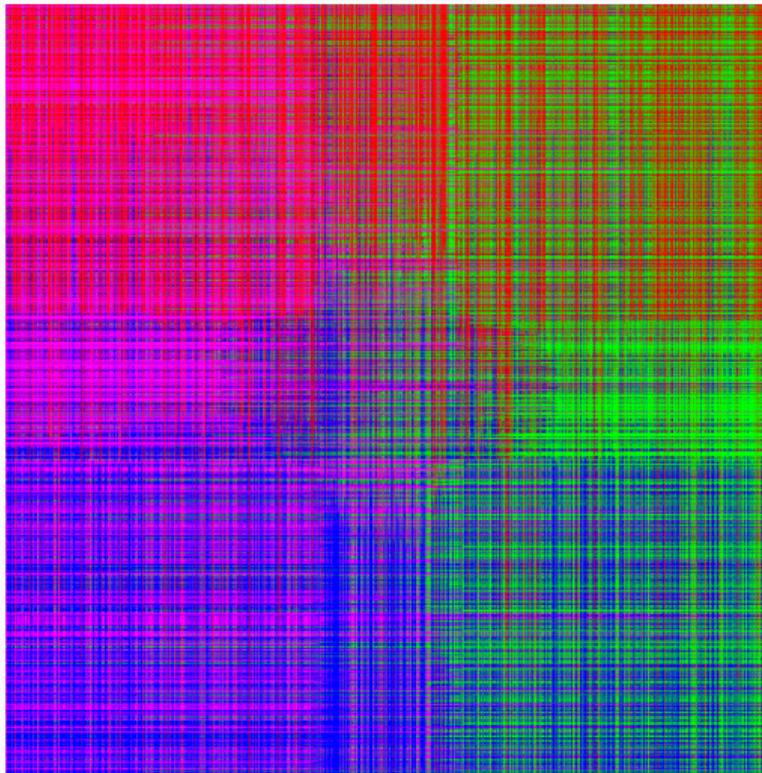
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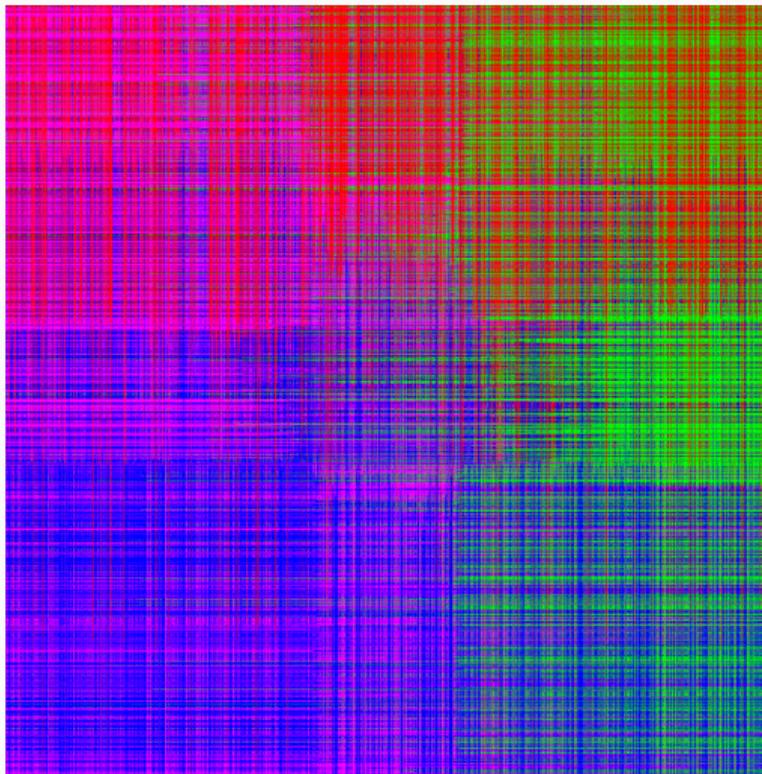
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  - For each level  $i$  in ascending order, determine how many you would miss by doing level  $i$  last instead of first:  $ans := ans + r_i - c_i$ .

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# H: Hunting the Mavericks

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Problem Author: Cristian-Alexandru Botocan

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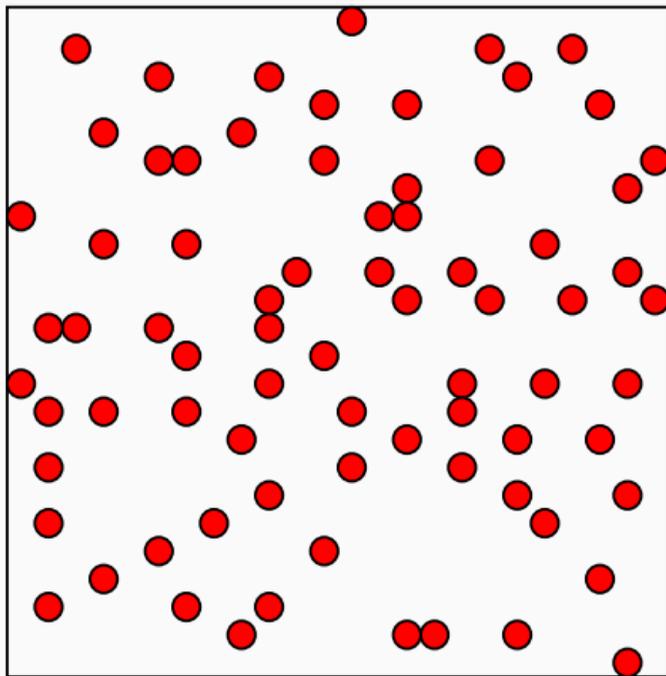
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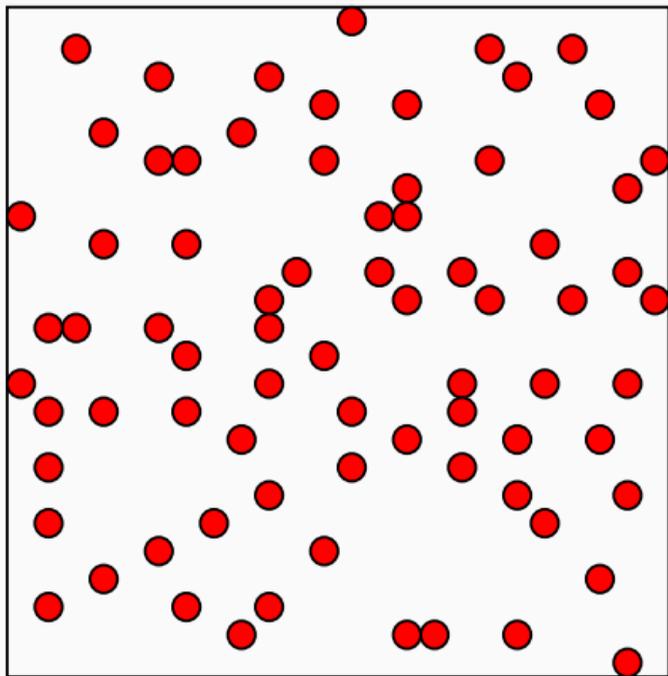
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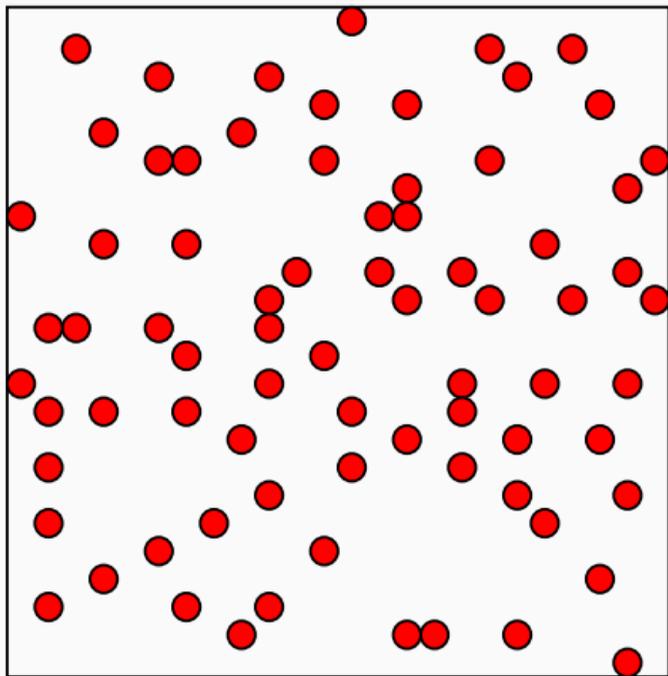
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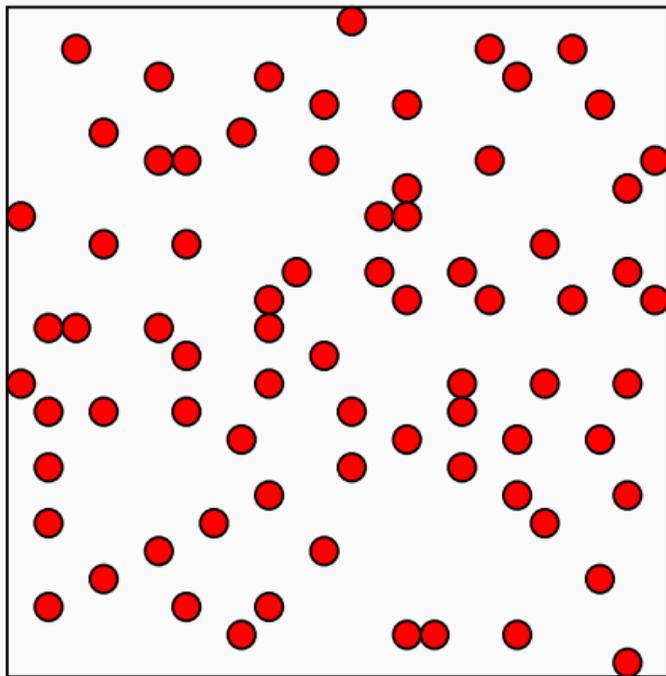
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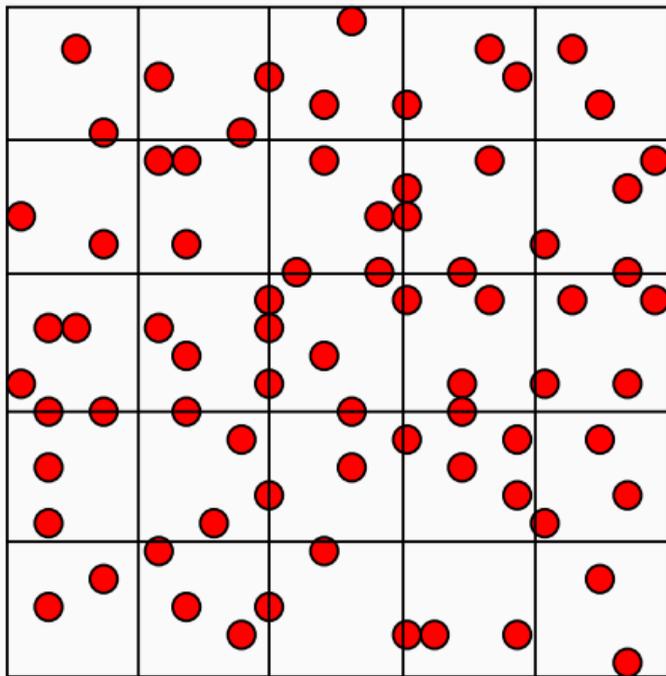
- **Problem:** Given a set of **uniform random** points in a square, find the smallest perimeter among all triangles.
- **Observation:** The points are randomly distributed, so there are no nasty testcases.
- How can we make use of this fact?



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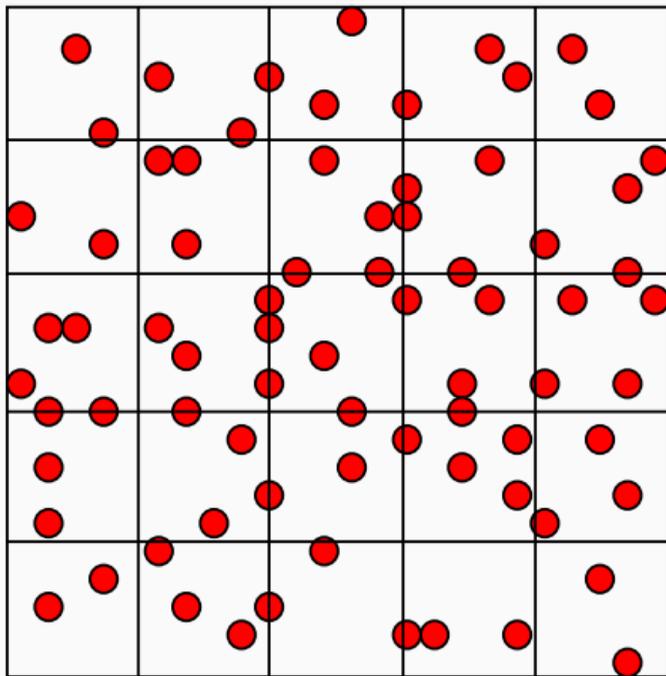
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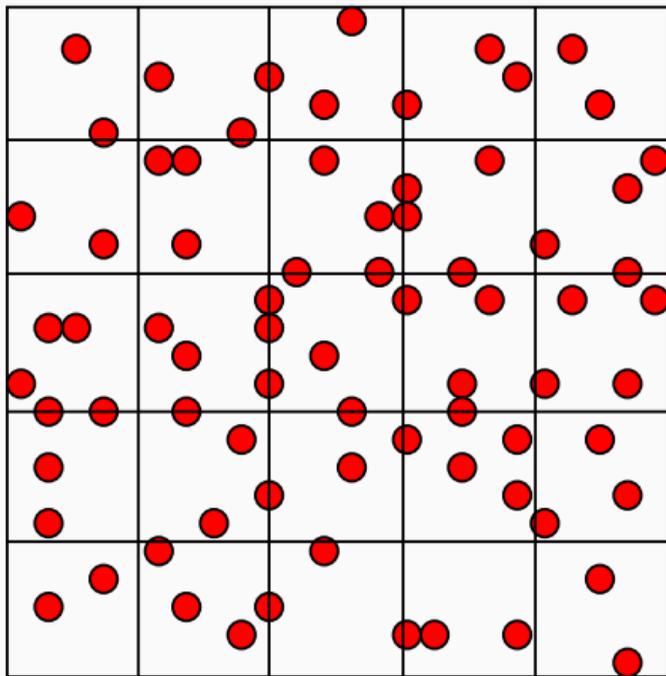
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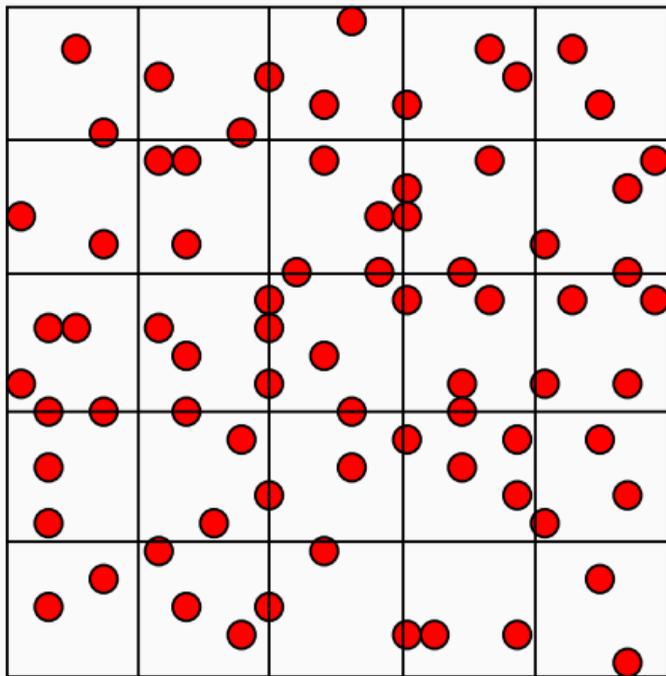
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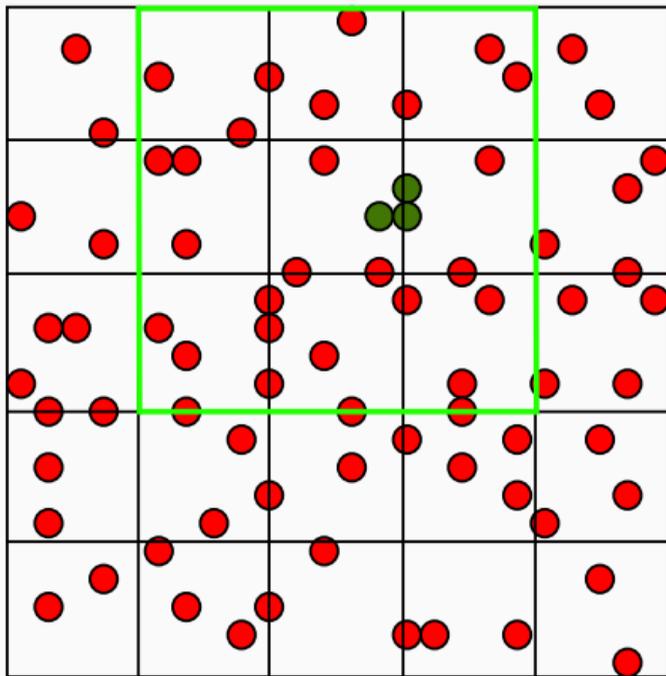
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- **Observation:** This means that the distance between two points of the smallest triangle can at most be  $(1 + \frac{1}{2}\sqrt{2}) \ell < 2\ell$ .



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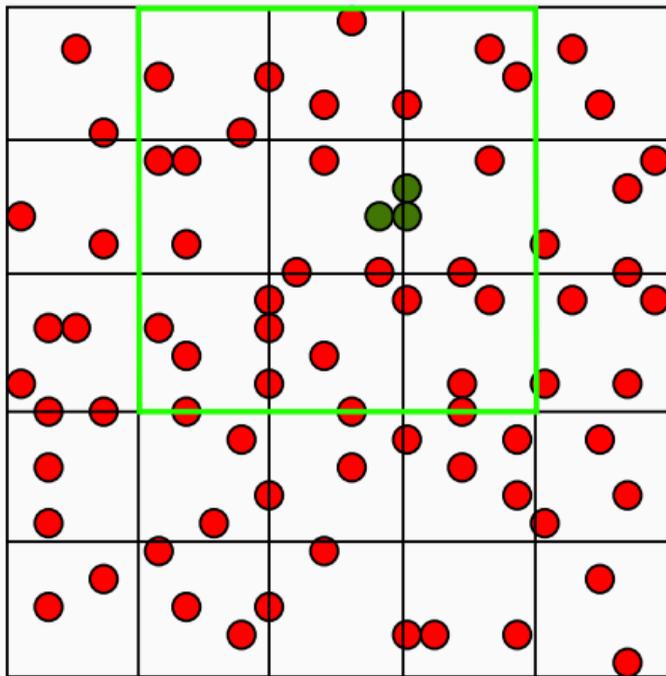
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- **Solution:** Calculate the perimeter of the triangles contained in all blocks of  $3 \times 3$  tiles.



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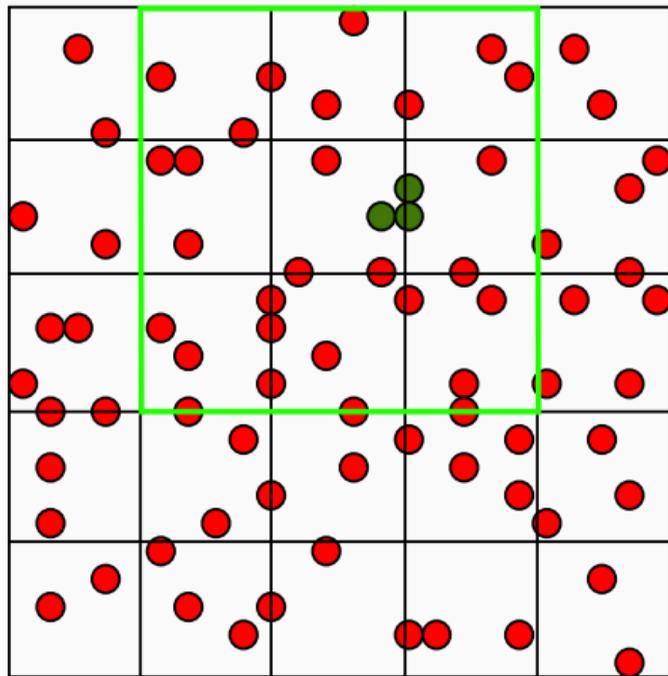
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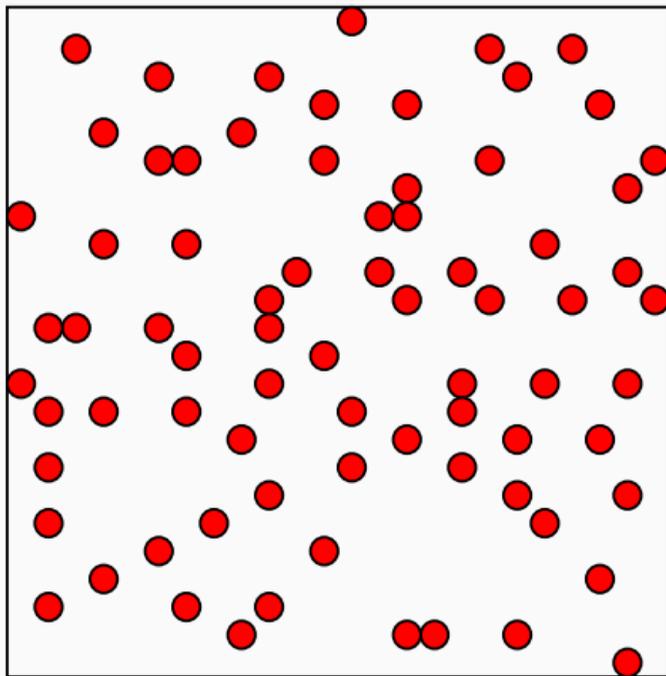
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- **Solution:** Because the points are uniformly distributed, the number of points inside the blocks is small with high probability.
- **Complexity:**  $\mathcal{O}(n)$ , with high probability.



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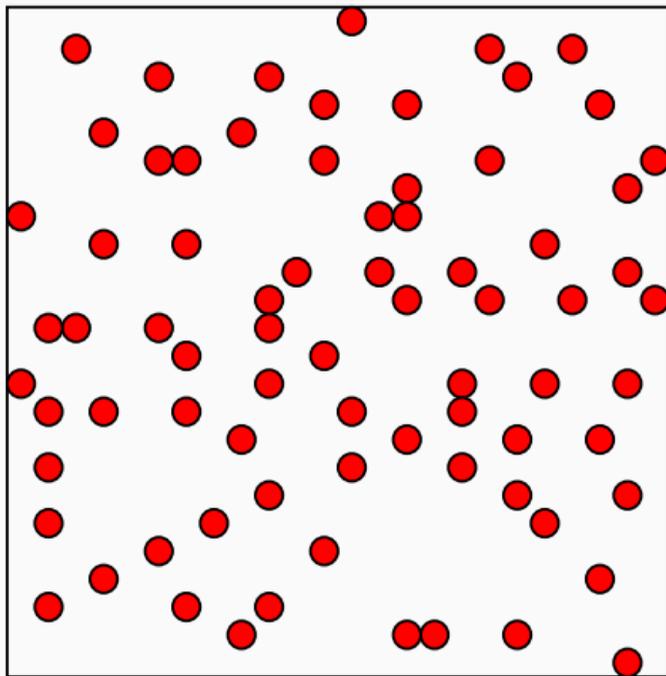
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### Jury work

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- The minimum<sup>1</sup> number of lines the jury needed to solve all problems is

$$4 + 6 + 5 + 9 + 1 + 22 + 24 + 5 + 3 + 5 = 84$$

On average 8.4 lines per problem, down from 10.4 last year

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## Thanks to:

### The Proofreaders

- Andrei Botocan (Bucharest, Romania)
- Davina van Meer (Delft)
- Michael Vasseur (VU Amsterdam)
- Michal Tešnar (RU Groningen)
- Nadyne Aretz (TU Delft)
- Thomas Verwoerd 📍 (TU Delft)
- Wietze Koops (RU Groningen)

### The Jury for FPC (TU Delft) and AAPJE (VU Amsterdam)

- Alexandru Bolfa (TU Delft)
- Angel Karchev (TU Delft)
- Jeroen Op de Beek (TU Delft)
- Leon van der Waal (TU Delft)
- Maarten Sijm (TU Delft)
- Matei Tinca (VU Amsterdam)
- Red Kalab (VU Amsterdam)